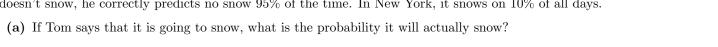
## Discussion 6C

CS 70, Summer 2024

## 1 Duelling Meteorologists

Tom is a meteorologist in New York. On days when it snows, Tom correctly predicts the snow 70% of the time. When it doesn't snow, he correctly predicts no snow 95% of the time. In New York, it snows on 10% of all days.





(c) Tom's friend Jerry is a meteorologist in Alaska. Jerry claims that she is a better meteorologist than Tom even though her overall accuracy is lower. After looking at their records, you determine that Jerry is indeed better than Tom at predicting snow on snowy days and sun on sunny day. Give an instance of the situation described above. Hint: Recall what we learned about Simpson's paradox. What is the weather like in Alaska, as compared to in New York?

## 2 Monty Hall's Revenge

Due to a quirk of the television studio's recruitment process, Monty Hall has ended up drawing all the contestants for his game show from among the ranks of former CS70 students. Unfortunately for Monty, the former students' amazing probability skills have made his cars-and-goats gimmick unprofitable for the studio. Monty decides to up the stakes by asking his contestants to generalize to three new situations with a variable number of doors, goats, and cars:

(a) There are n doors for some n > 2. One has a car behind it, and the remaining n - 1 have goats. As in the ordinary Monty Hall problem, Monty will reveal one door with a goat behind it after you make your first selection. Compute the probability of winning if you switch, as well as the probability of winning if you don't switch, and compare the results.

(Hint: Think about the size of the sample space for the experiment where you *always* switch. How many of those outcomes are favorable?)

(b) Again there are n > 2 doors, one with a car and n - 1 with goats, but this time Monty will reveal n - 2 doors with goats behind them instead of just one. How does switching affect the probability of winning in this modified scenario?

(c) Finally, imagine there are k < n-1 cars and n-k goats behind the n > 2 doors. After you make your first pick, Monty will reveal j < n-k doors with goats. What values of j, k maximize the relative improvement in your probability of winning if you choose to switch? (i.e. what j, k maximizes the ratio between your probability of winning when you switch, and your probability of winning when you do not switch?)